

## Volumes of Solids with Known Cross Sections CW/HW

1. A solid  $S$  is built in such a way that its base is bounded by a circle of radius 3 meters and center at the origin. If each plane section perpendicular to a given diameter of the base is a square, find the volume of solid  $S$ .
2. Find the volume of a solid  $S$  if its base is bounded by the ellipse  $x^2 + 4y^2 = 4$  and the cross sections perpendicular to the  $x$ - axis are squares.
3. Find the volume of a solid  $S$  if its base is bounded by the circle  $x^2 + y^2 = 1$  and the cross sections perpendicular to the  $x$ - axis are equilateral triangles.
4. Find the volume of a solid  $S$  if its base is bounded by the circle  $x^2 + y^2 = 4$  and the cross sections perpendicular to the  $x$ - axis are semicircles.
5. Find the volume of a solid  $S$  if its base is bounded by the circle  $x^2 + y^2 = 16$  and the cross sections perpendicular to the  $x$ - axis are isosceles right triangles having the hypotenuse in the plane of the base.
6. Find the volume of a solid  $S$  if its base is bounded by the curve  $y = 2x^3$ , the lines  $x = 2$  and  $y = 0$ , and the cross sections perpendicular to the line  $x = 0$  are equilateral triangles.

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|----|---------|----|-----------------|----|-----------------|----|-----------|
| 1. | 144     | 2. | $32/3$          | 3. | $(4\sqrt{3})/3$ | 4. | $16\pi/3$ |
| 5. | $256/3$ | 6. | $(8\sqrt{3})/5$ |    |                 |    |           |