

Good afternoon: warm up

Find $f'(3)$ if $f(x)=\text{arcsec}(x^2)$

$$f'(x) = \frac{1}{(x^2)\sqrt{(x^2)^2-1}} \cdot 2x$$

$$f'(x) = \frac{2x}{x^2\sqrt{x^4-1}}$$

$$f'(3) = \frac{6}{9\sqrt{80}} \rightarrow \frac{2}{3\sqrt{80}}$$

$$\frac{d}{dx} \text{arcsec}(x) = \frac{1}{|x|\sqrt{x^2-1}}$$
$$\frac{d}{dx} \text{arccsc}(x) = \frac{1}{|x|\sqrt{x^2-1}}$$

$$\frac{2}{3 \cdot 4\sqrt{5}}$$

$$\frac{2}{12\sqrt{5}}$$

$$\frac{1}{6\sqrt{5}}$$

~~Handwritten scribbles and corrections in green ink.~~

HW

answers posted to mcalc.weebly.com

questions on a few in particular?

$$601. \quad y = (\cos 3x)^2 - (\sin 3x)^2$$

$$y' = 2(\cos 3x)' \cdot \sin(3x) - 2(\sin(3x))' \cdot \cos(3x)$$

$$= 6 \cos(3x) \sin(3x) - 6 \cos(3x) \sin(3x)$$

$$= 12 \cos(3x) \sin(3x)$$

584.)

$$B(x) = \frac{x-2}{\ln x}$$

597.)

$$y = \frac{\cot(5x)}{3x^2}$$

Low Dhi - Hd: low
Low: Low

$$\frac{dy}{dx} = \frac{-\csc^2(5x) \cdot 5 \cdot 3x^2 - \cot(5x) \cdot 6x}{9x^4}$$

$$\frac{-15x^2 \csc^2(5x) - 6x \cdot \cot(5x)}{9x^4}$$

$$\frac{-5x \cdot \csc^2(5x) - 2 \cot(5x)}{3x^3}$$

A return to differentiability

Why is $y = \sqrt[5]{3x}$ not differentiable at $x=0$?

Is this continuous? *yes: odd radical*

ex $y = \sqrt[4]{3x}$ doesn't accept neg.

Is its derivative cont.?

$$y = (3x)^{1/5}$$

$$\frac{dy}{dx} = ?$$

$$= \frac{1}{5} (3x)^{-4/5} \cdot 3$$

$$\frac{3}{5} (3x)^{-4/5} \rightarrow$$

$$\frac{3}{5 (3x)^{4/5}} \rightarrow \frac{3}{5 \sqrt[5]{(3x)^4}}$$

$x \neq 0$

No.
Not cont.
@ $x=0$

Show why each is nondifferentiable at $x=0$

$$f(x) = \sqrt[3]{4x^2} = (4x^2)^{1/3}$$

fis
cont.

$$f'(x) = \frac{1}{3} (4x^2)^{-2/3} \cdot 8x$$

$$f'(x) = \frac{8x}{3 \sqrt[3]{(4x^2)^2}}$$

$x=0$ gives you $\frac{8 \cdot 0}{3 \cdot 0}$
 $= \frac{0}{0}$ (3)

$f'(x)$ is not cont.
So f is not diff.

cont.

$$g(x) = -|x| + 5$$

$$g(x) = \begin{cases} x+5, & x \leq 0 \\ -x+5, & x > 0 \end{cases}$$



$|x| \Rightarrow \begin{cases} x, & x \geq 0 \\ -x, & x < 0 \end{cases}$

$g'(x) = \begin{cases} 1, & x < 0 \\ -1, & x > 0 \end{cases}$

Not.
Cont.