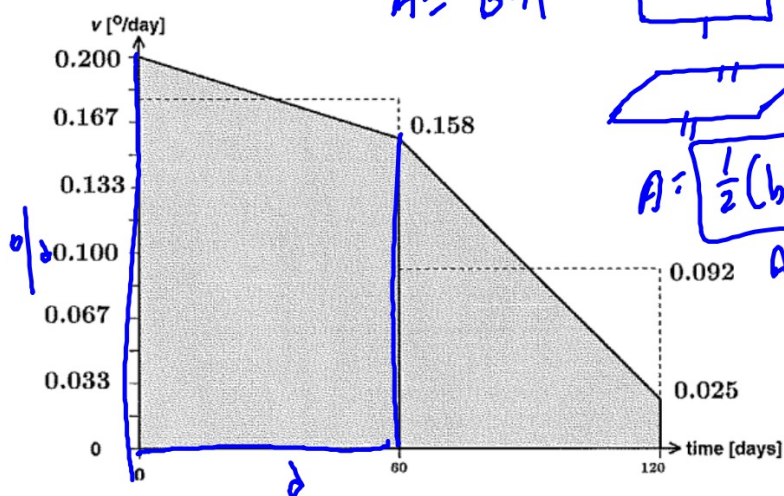


AP Calculus AB

Warm up: answer the Jupiter travel problem from the Cuneiform tablets on Wednesday

Ancient Babylonians measured the change in location of Jupiter over 120 days. They measured the change in degrees per day along its path in the sky. Here is their data transcribed from their Cuneiform tablets dating back to ~300BCE.

Through how many degrees did Jupiter travel during the 120 days?



AP Calculus AB

Riemann Sum Hw solutions

25. Left: 13 Right: 15

26. L: $37/3$ 12.333

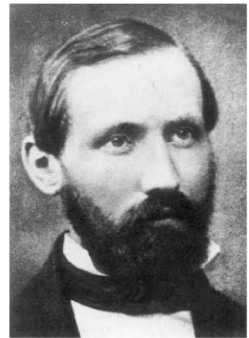
 R: $35/3$ 11.667

27. L: 55

 R: 74.5

28. L: 9.688

 R: 11.688

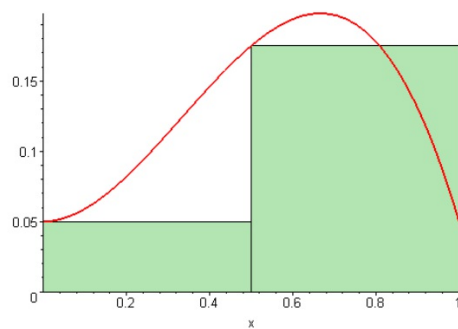


Riemann integral

From Wikipedia, the free encyclopedia

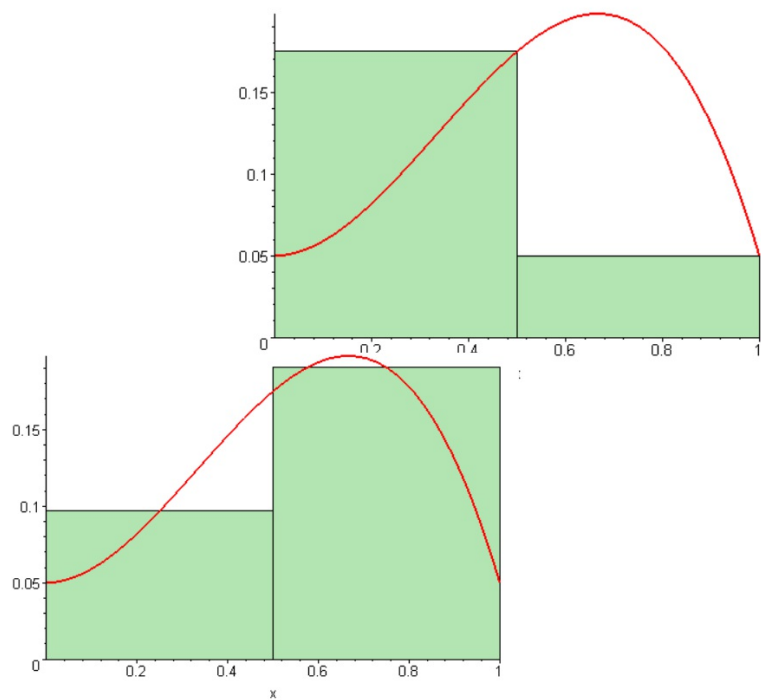
In the branch of [mathematics](#) known as [real analysis](#), the **Riemann integral**, created by [Bernhard Riemann](#), was the first rigorous definition of the [integral](#) of a [function](#) on an [interval](#).^[1] For many functions and practical applications, the Riemann integral can be evaluated by the [fundamental theorem of calculus](#) or approximated by [numerical integration](#).

Visuals of Riemann Sums



http://webpace.ship.edu/msrenault/GeoGebraCalculus/integration_riemann_sum.html

CIM



MRAM

Cleaned up version on next pg

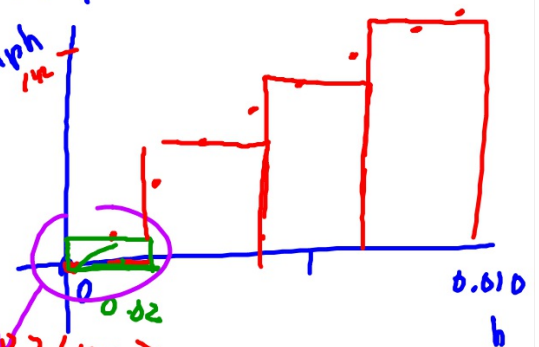
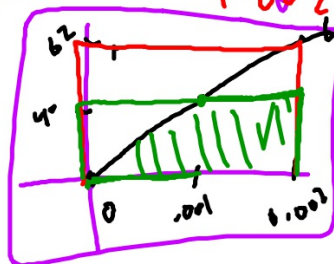
Staple to notes

921. The table shows the velocity of a vintage sports car accelerating from 0 to 142 miles per hour in 36 seconds (0.001 hours).

hours	0.000	0.001	0.002	0.003	0.004	0.005	0.006	0.007	0.008	0.009	0.010
mph	0	40	62	82	96	108	116	125	132	137	142

- a) Use a Riemann sum to estimate how far the car traveled during the 36 seconds it took to reach 142 mph.
- b) Roughly how many seconds did it take the car to reach the halfway point? About how fast was the car going then?

Base: Δx height $f(\text{Midpoint})$
 $0.002 \cdot 40 + 0.002 \cdot 82 + 0.002 \cdot 108 + 0.002 \cdot 125 + 0.002 \cdot 137$
 one rectangle



Midpoint Riemann Sum with a table

921. The table shows the velocity of a vintage sports car accelerating from 0 to 142 miles per hour in 36 seconds (0.01 hours).

hours	0.000	0.001	0.002	0.003	0.004	0.005	0.006	0.007	0.008	0.009	0.010
mph	0	40	62	82	96	108	116	125	132	137	142

a) Use a Riemann sum to estimate how far the car traveled during the 36 seconds it took to reach 142 mph.

b) Roughly how many seconds did it take the car to reach the halfway point? About how fast was the car going then?

If we use 5 intervals, midpoint will be easy to find.

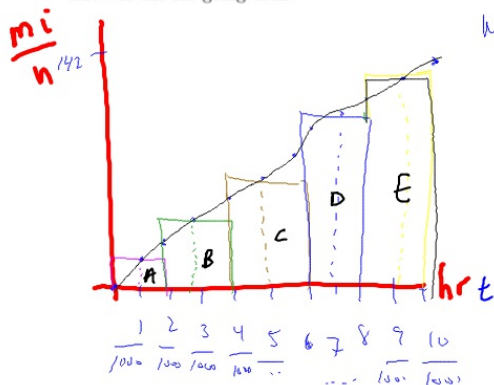
Each interval's

width is

0.002 seconds long

(base of rectangle

$$\sum \underbrace{0.002}_{\Delta t} \cdot f(\text{midpoint of each interval})$$



Area of A:

Area of B

C

D

E

$$0.002 \cdot [40 \text{ m/h}] + 0.002[82] + 0.002(108) + 0.002(125) + 0.002(137)$$

base · height

Since Δx is all 0.002, can factor that out!

$$0.002(40 + 82 + 108 + 125 + 137)$$

$$0.002(492)$$

$$0.984 \text{ miles}$$

921. The table shows the velocity of a vintage sports car accelerating from 0 to 142 miles per hour in 36 seconds (0.01 hours).

hours	0.000	0.001	0.002	0.003	0.004	0.005	0.006	0.007	0.008	0.009	0.010
mph	0	40	62	82	96	108	116	125	132	137	142

midpoint

- a) Use a Riemann sum to estimate how far the car traveled during the 36 seconds it took to reach 142 mph.

- b) Roughly how many seconds did it take the car to reach the halfway point? About how fast was the car going then?

Distance = time · rates

$$\frac{0.984}{2} = 0.492 \text{ miles}$$

$$\frac{0.492}{0.002} = 0.002 (\sum f)$$

$$246 = \sum f(\text{midpoints})$$

$40 + 82 + 108 \leftarrow$

> 230

$$40 + 82 + 108 + 125$$

$$< 355$$

So, between 0.005 hr and 0.007 hr

probably 0.006 hr

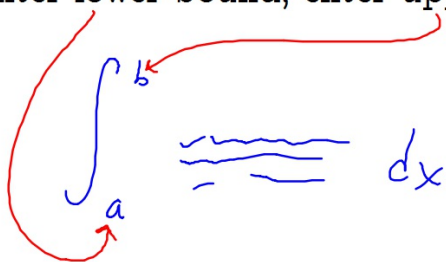
$$0.006 \text{ hr} \cdot \frac{3600 \text{ sec}}{1 \text{ hr}} = 21.6 \text{ sec}$$

Area under derivative gives anti-derivative

http://webspace.ship.edu/msrenault/GeoGebraCalculus/integration_area_function.html

Calculator Methods

- put function you want definite integral of in y1
- graph it
- 2nd TRACE (calc menu) choice 7 is definite integral
- enter lower bound, enter upper bound, hit enter



A hand-drawn diagram illustrating the notation for a definite integral. On the left, a large blue integral symbol \int is shown. A red arrow curves from the lower bound 'a' at the bottom of the symbol to the text 'enter lower bound' in the list above. Another red arrow curves from the upper bound 'b' at the top of the symbol to the text 'enter upper bound' in the list above. To the right of the integral symbol, the differential dx is written in blue, with three horizontal wavy lines above it.

Can you make the calculator give you a negative answer?

either use: $\left\{ \begin{array}{l} - \text{area below} \\ \text{x-axis} \\ - \text{invert bounds} \\ \text{so that } a > b \end{array} \right.$

$$\int_0^3 e^x \cdot dx \approx 19.588$$

$$e^3 - e^0 = e^3 - 1$$

$$\int_a^b f(x) dx$$

Practice with both Riemann Sums and Definite Integration



Back of snowfall handout
from Wednesday

(Just like hw
due today)



Back of stapled packet from last Friday

See mcalc.
videos

Integrals Test Study Guide

→ letter answers

on
mcalc.weebly.com.

HW due ~~Wed~~ ^{Fri.}

p. 274:

#47

p. 288

#5-30 (x3), 67