

Good afternoon: do these 4 AP no calculator multiple choice problems

$$\int_0^{\frac{\pi}{4}} \sin x \, dx =$$

- (A)  $-\frac{\sqrt{2}}{2}$       (B)  $\frac{\sqrt{2}}{2}$       (C)  $-\frac{\sqrt{2}}{2} - 1$       (D)  $-\frac{\sqrt{2}}{2} + 1$       (E)  $\frac{\sqrt{2}}{2} - 1$

$$\int x^2 \cos(x^3) \, dx =$$

- (A)  $-\frac{1}{3} \sin(x^3) + C$   
(B)  $\frac{1}{3} \sin(x^3) + C$   
(C)  $-\frac{x^3}{3} \sin(x^3) + C$   
(D)  $\frac{x^3}{3} \sin(x^3) + C$   
(E)  $\frac{x^3}{3} \sin\left(\frac{x^4}{4}\right) + C$

If  $f(x) = \ln(x + 4 + e^{-3x})$ , then  $f'(0)$  is

- (A)  $-\frac{2}{5}$       (B)  $\frac{1}{5}$       (C)  $\frac{1}{4}$       (D)  $\frac{2}{5}$       (E) nonexistent

$$\frac{d}{dx} \left( \int_0^{x^2} \sin(t^3) \, dt \right) =$$

- (A)  $-\cos(x^6)$       (B)  $\sin(x^3)$       (C)  $\sin(x^6)$       (D)  $2x \sin(x^3)$       (E)  $2x \sin(x^6)$

$$\int_0^{\pi/4} \sin x \, dx =$$

(A)  $-\frac{\sqrt{2}}{2}$

(B)  $\frac{\sqrt{2}}{2}$

(C)  $-\frac{\sqrt{2}}{2} - 1$

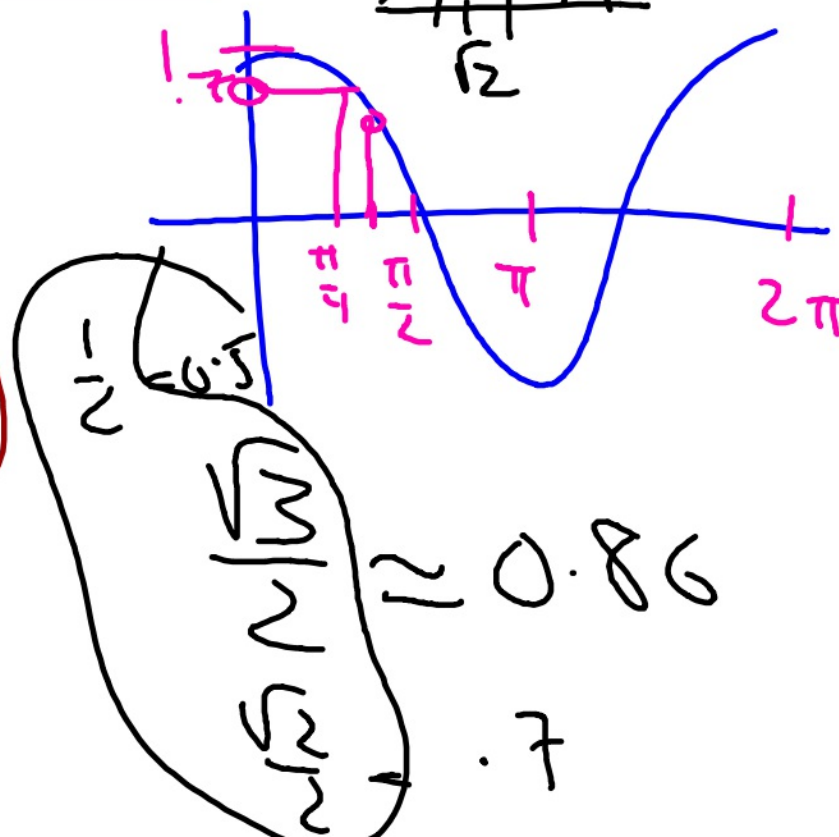
(D)  $-\frac{\sqrt{2}}{2} + 1$

(E)  $\frac{\sqrt{2}}{2} - 1$



$$[-\cos x]_0^{\pi/4}$$

$$\left( -\cos \frac{\pi}{4} \right) - \left( -\cos 0 \right)$$
$$-\frac{\sqrt{2}}{2} + 1$$



$$\int x^2 \cos(x^3) dx =$$

(A)  $-\frac{1}{3} \sin(x^3) + C$

(B)  $\frac{1}{3} \sin(x^3) + C$

(C)  $-\frac{x^3}{3} \sin(x^3) + C$

(D)  $\frac{x^3}{3} \sin(x^3) + C$

(E)  $\frac{x^3}{3} \sin\left(\frac{x^4}{4}\right) + C$

~~$\int x^2 \cdot \cos(x^3) dx$~~

$\int \cos(x^3) dx$

what:  $3x^2$

$\int \sin(x^3) + C$

If  $f(x) = \ln(x + 4 + e^{-3x})$ , then  $f'(0)$  is

- (A)  $-\frac{2}{5}$  (B)  $\frac{1}{5}$  (C)  $\frac{1}{4}$  (D)  $\frac{2}{5}$  (E) nonexistent

$$f' = \frac{1}{x + 4 + e^{-3x}} \cdot (1 + 0 + e^{-3x} \cdot -3)$$

@  $x=0$

$$\frac{1}{4 + \cancel{e^0}} \cdot (1 - 3\cancel{e^0})$$

$$\frac{1}{5} \cdot -2$$

$$\frac{d}{dx} e^{f(x)} = e^{f(x)} \cdot f'(x)$$

$$3^3 = 27$$

$$3^2 = 9$$

$$3^1 = 3$$

$$\rightarrow 3^0 = 1$$

$$3^{-1} = \frac{1}{3}$$

$$\frac{d}{dx} \left( \int_0^{x^2} \sin(t^3) dt \right) =$$

- (A)  $-\cos(x^6)$     (B)  $\sin(x^3)$     (C)  $\sin(x^6)$     (D)  $2x \sin(x^3)$     (E)  $2x \sin(x^6)$

$$\sin((x^2)^3) \cdot 2x$$

$$2x \cdot \sin(x^6)$$

HW questions?

Which Saturday for AP test?

~~4/6~~\*

4/13

4/20

✓ 9 AM

4/27

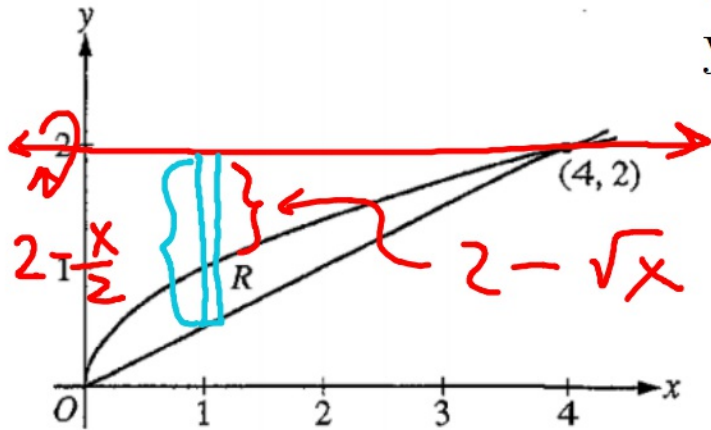
~~5/4~~

5/11

More with volume:

$$y = \sqrt{x}$$

$$y = x/2$$



①

$$\int_0^4 x^{1/2} - \frac{1}{2}x \, dx$$

$$\left[ \frac{2}{3}x^{3/2} - \frac{1}{4}x^2 \right]_0^4$$

$$\left( \frac{16}{3} - \frac{12}{4} \right) - (0)$$

$$\left( \frac{16}{3} - 3 \right)$$

$$\frac{7}{3}$$

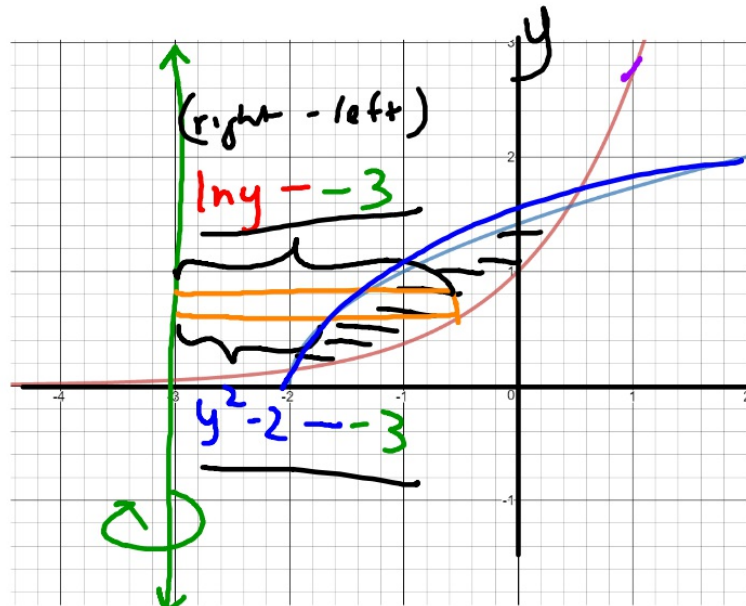
① Find area of R (no calc)

② Revolve R around  $y=2$  (calc)

$$V = \pi \int_0^4 \left( 2 - \frac{x}{2} \right)^2 - \left( 2 - \sqrt{x} \right)^2 \, dx$$

$\left( \frac{7}{3} \right)$   
 $\left( \frac{7}{3} \pi \right)$

# Vertical axis revolutions



•  $y = e^x$

•  $y = \sqrt{x+2}$

$(-1.961, 0.138)$   
 $(0.448, 1.564)$

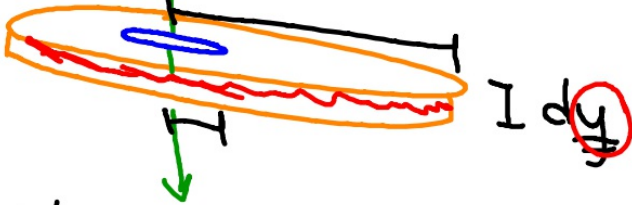
about  $x = -3$

•  $\ln y = \ln e^x$

$\ln y = x$

•  $y = \sqrt{x+2}$

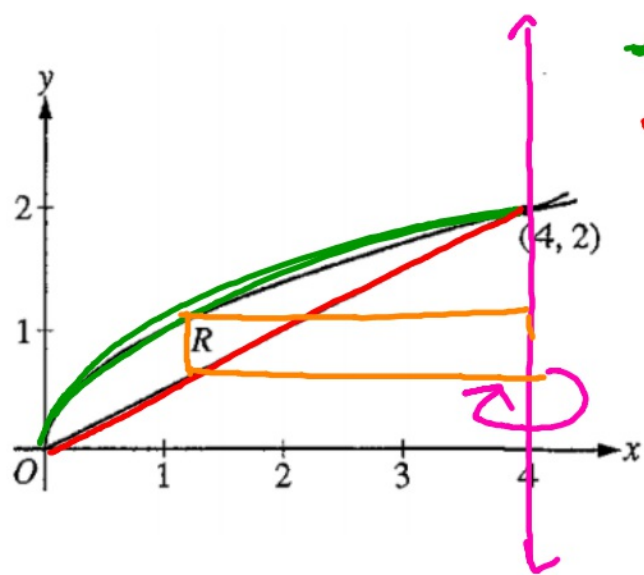
$y^2 = x+2 \rightarrow \underline{y^2 - 2 = x}$



$V = \pi (\ln y + 3)^2 dy - \pi (y^2 + 1)^2 dy$

$V = \pi \int_{0.138}^{1.564} (\ln y + 3)^2 - (y^2 + 1)^2 dy$





- $y = \sqrt{x}$

- $y = x/2$

- $y^2 = x$

- $2y = x$

Revolve R about  $x=4$

$$V = \pi \int_0^2 (4 - y^2)^2 - (4 - 2y)^2 dy$$

Volume by cross section