

AP Calculus DS

Assessments from Monday are being passed back

Absent Monday? You will take it soon--I will return them to you asap so you know if you need to re-assess

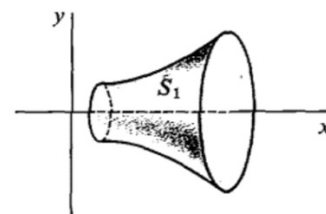
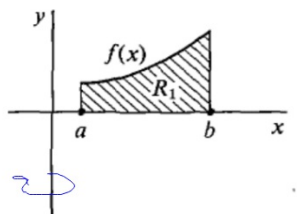
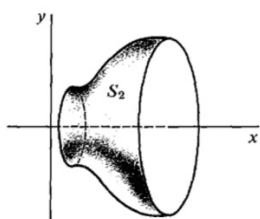
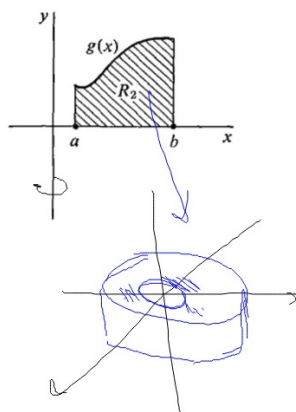
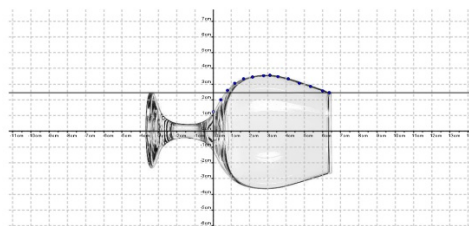
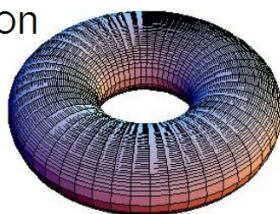
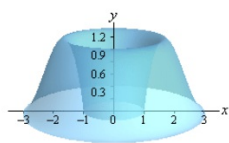
This DS is for you to re-assess whatever is needed. Please know what skills you need and have the homework out for me to check.

No reassessments? Work on/double check AP q's due today.

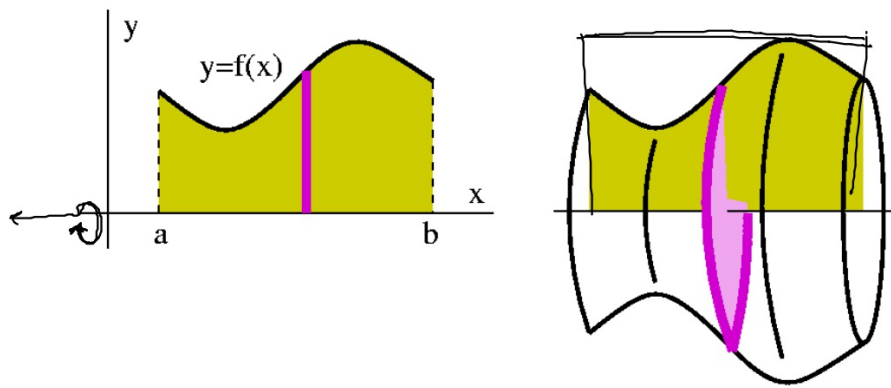
Bring colored pencils if you prefer to use your own

turn scantrons in please

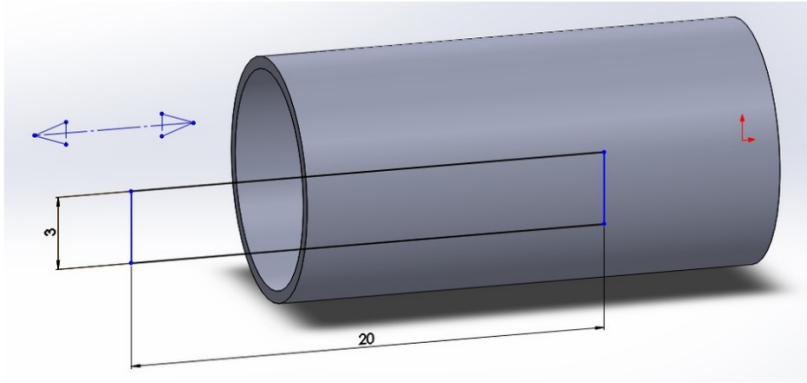
Volume of Revolution



Volumes of Solids of Revolution (Disk method)

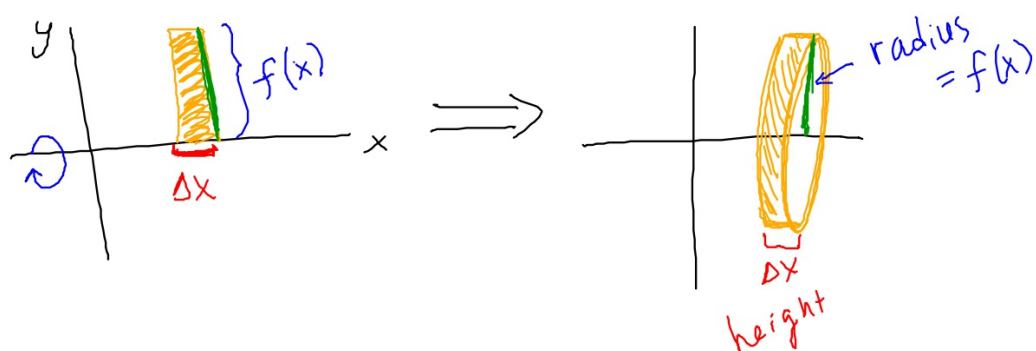


What happens when you revolve a rectangle around an axis?

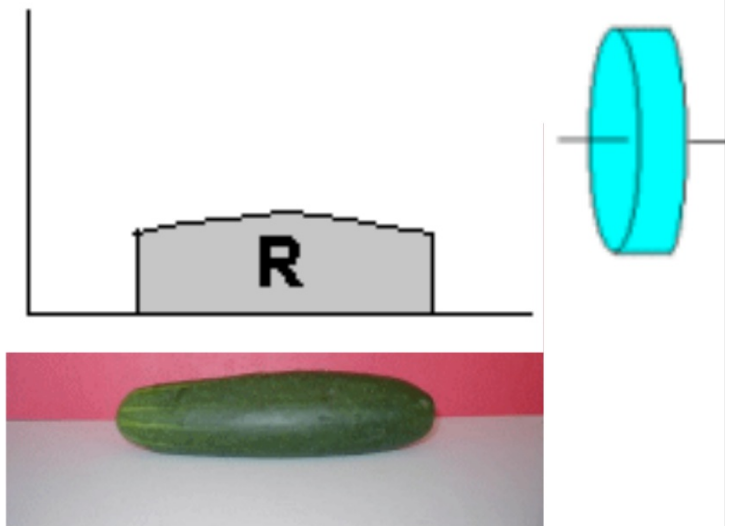
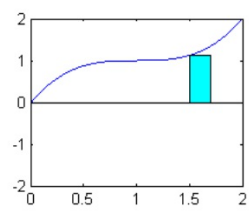
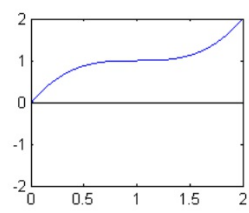


So a single rectangle becomes a cylindrical "disk"

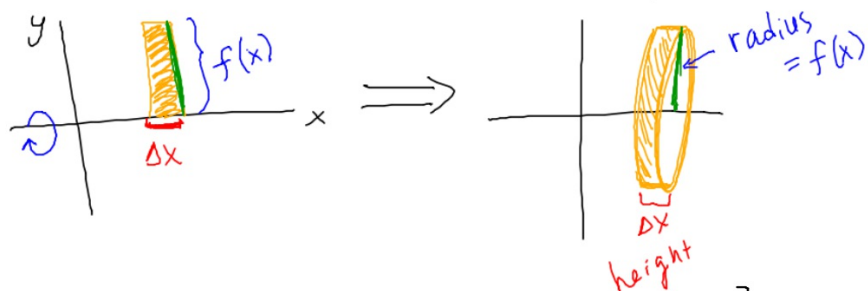
What is its radius? What is its height/depth?







Volume of solid = sum of volume of slices



$$V_{\text{cyl}} = \pi r^2 \cdot h$$

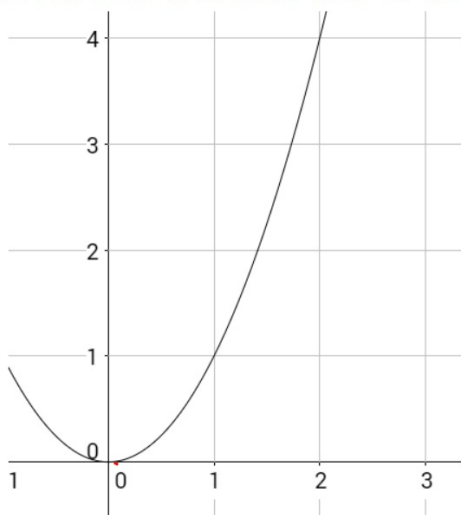
Volume of one disk = $\pi \cdot [f(x)]^2 \cdot \Delta x$

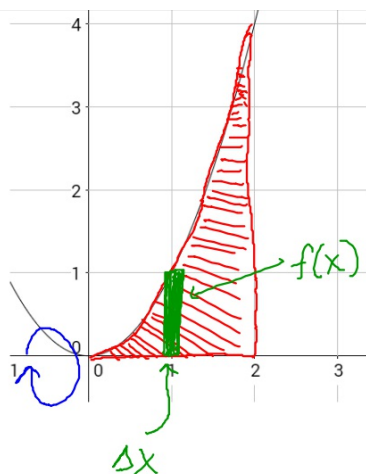
\uparrow radius \uparrow height

$V = \text{Sum of all disks} = \int_a^b \pi \cdot [f(x)]^2 \cdot dx$

Get some colored pencils

Concrete Example: Region bounded $y = x^2$, x-axis, and $x=2$ revolved around the x-axis.

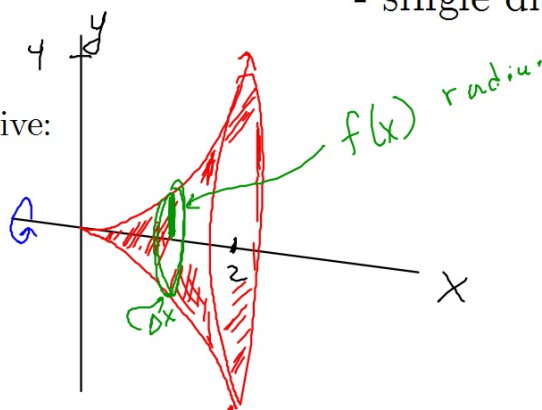




$y = x^2$, x -axis, $x = 2$
are bounds,
Revolve around x -axis.

Always sketch:
- revolution axis
- single rectangle
- single disk

In perspective:



$$V = \int_0^2 \pi \cdot (x^2)^2 \cdot dx$$

$$\pi \int_0^2 x^4 \cdot dx$$

$$\pi \left[\frac{1}{5} x^5 \right]_0^2$$

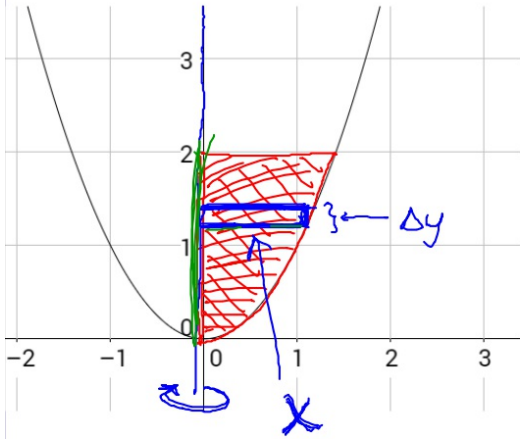
$$\pi \left(\frac{32}{5} \right) \Rightarrow \frac{32}{5} \pi$$

Axes of Revolution: x-axis (just did it)

y-axis (about to do it)

other vertical + horizontal lines (~~tonight's hw~~ video)

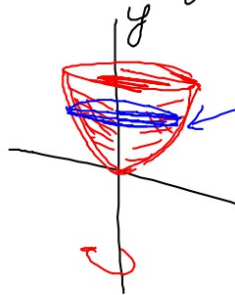
<http://www.geogebra.org/material/show/id/18475>



Revolve about the y-axis

$$y = x^2 \iff x = \sqrt{y}$$

$y = 2$ is a boundary along w/ y-axis.



$$V = \pi \cdot x^2 \cdot \Delta y$$

$$V = \int_0^2 \pi x^2 dy$$

$$+ \int_0^2 \pi \cdot (\sqrt{y})^2 dy$$

$$\int_0^2 \pi \cdot y \cdot dy$$

$$\pi \left[\frac{1}{2} y^2 \right]_0^2$$

$$\pi \left[\frac{1}{2} \cdot 4 - 0 \right]$$

$$2\pi$$

Homework: p. 453 # 3, 4, 7, 8