

1. The function F above satisfies the conclusion of Rolle's Theorem in the interval [a, b] because

- I. F is continuous. F is differentiable on (a, b). II. F(a) = F(b) = 0.III. Rolle's Theorem A) I only is the MVT where B) II only f(b)-f(a) =0C) I and III only b-a D) I, II, and III
- E) F does not satisfy Rolle's Theorem

2. If $Q(x) = (3x+2)^3$, then the third derivative of Q at x = 0 is

- **A)** 0
- **B**) 9
- **C)** 54
- **D)** 162
- **E)** 224

3. If a function g is differentiable on the interval [-4, 4], then which of the following statements is true?

- A) g is not continuous on [-5, 5].
- **B)** g is not differentiable on [-5, 5].
- C) g'(c) = 0 for some c in [-4, 4].
- D) The conclusion of the Mean Value Theorem applies to g.
- E) None of the above statements are true.

4. The value of c guaranteed to exist by the Mean Value Theorem for $f(x) = x^2$ in the interval [0,3] is

- **A)** 1
- **B)** 2
- **C)** $\frac{3}{2}$
- **D**) $\frac{1}{2}$
- E) None of these



5. The graph of the derivative of a function f is shown above. Which of the following are true about the original function f?

- I. f is increasing on the interval (-2, 1).
- II. f is continuous at x = 0.
- III. f has an inflection point at x = -2.
- A) I only
- B) II only
- C) III only
- D) II and III only
- E) I, II, and III

6. Two particles move along the x-axis and their positions at time $0 \le t \le 2\pi$ are given by $x_1 = \cos t$ and $x_2 = e^{(t-3)/2} - 0.75$. For how many values of t do the two particles have the same velocity?

- **A)** 0
- **B)** 1
- **C)** 2
- **D)** 3
- **E)** 4



7. The conical reservoir shown above has diameter 12 feet and height 4 feet. Water is flowing into the reservoir at the constant rate of 10 cubic feet per minute. At the instant when the surface of the water is 2 feet above the vertex, the water level is rising at the rate of

- A) 0.177 ft per min
- **B)** 0.354 ft per min
- **C)** 0.531 ft per min
- D) 0.708 ft per min
- E) 0.885 ft per min

8. The position of a particle moving on the x-axis, starting at time t = 0, is given by $x(t) = (t-a)^3(t-b)$, where 0 < a < b. Which of the following statements are true?

- I. The particle is at a positive position on the x-axis at time $t = \frac{a+b}{2}$.
- II. The particle is at rest at time t = a.
- III. The particle is moving to the right at time t = b.
- A) I only
- B) II only
- C) III only
- D) I and II only
- E) II and III only

9. Let the function f be differentiable on the interval [0, 2.5] and define g by g(x) = f(f(x)). Use the table below to estimate g'(1).

| x | 0.0 | 0.5 | 1.0 | 1.5 | 2.0 | 2.5 |
|------|-----|-----|-----|-----|-----|-----|
| f(x) | 1.7 | 1.8 | 2.0 | 2.4 | 3.1 | 4.4 |

- **A)** 0.8
- **B)** 1.2
- **C)** 1.6
- **D)** 2.0
- **E)** 2.4

10. Which of the following are true about a particle that starts at t = 0 and moves along a number line if its position at time t is given by $s(t) = (t-2)^3(t-6)$?

- I. The particle is moving to the right for t > 5.
- II. The particle is at rest at t = 2 and t = 6.
- III. The particle changes direction at t = 2.
- A) I only
- B) II only
- C) III only
- D) I and III only
- E) None are true.



11. The graph of the function f is shown above. Which of the following statements are true?

I.
$$\lim_{h \to 0} \frac{f(2+h) - f(2)}{h} = f'(5).$$

II.
$$\frac{f(5) - f(2)}{5 - 2} = \frac{2}{3}.$$

III.
$$f''(1) \le f''(5).$$

- A) I and II only
- B) I and III only
- C) II and III only
- D) I, II, and III
- E) None of these

12. If
$$x^2 - y^2 = 25$$
, then $\frac{d^2 y}{dx^2} =$
A) $-\frac{x}{y}$ B) $\frac{5}{y^2}$ C) $-\frac{x^2}{y^3}$ D) $-\frac{25}{y^3}$ E) $\frac{4}{y^3}$



13. A rectangle with one side on the x-axis has its upper vertices on the graph of $y = 4 - x^2$, as shown in the figure above. What is the maximum area of the rectangle?

- A) 1.155
- **B)** 1.855
- **C)** 3.709
- **D)** 6.158
- **E)** 12.316

14. Let f be a twice-differentiable function of x such that, when x = c, f is decreasing, concave up, and has an x-intercept. Which of the following is true?

- A) f(c) < f'(c) < f''(c)
- **B)** f(c) < f''(c) < f'(c)
- **C)** f'(c) < f(c) < f''(c)
- D) f'(c) < f''(c) < f(c)
- E) f''(c) < f(c) < f'(c)

15. If $f'(x) = \arctan(x^3 - x)$, at how many points is the tangent line to the graph of f(x) parallel to the line y = 2x?

A) None

- **B)** 1
- **C)** 2
- **D)** 3
- E) Infinitely many