

Good afternoon: warm up in notebooks.

Evaluate the limit. Do as little work as needed.

$$\left\{ \frac{d}{dx} x^n = nx^{n-1} \right.$$

$$\lim_{\Delta x \rightarrow 0} \frac{(x + \Delta x)^3 - 3(x + \Delta x)^4 + 2(x + \Delta x) - \underbrace{(x^3 - 3x^4 + 2x)}_{f(x)}}{\Delta x}$$

$f'(x)$?

$f(x)$

$$f'(x) = \lim_{\Delta x \rightarrow 0} \frac{f(x + \Delta x) - \underline{f(x)}}{\Delta x}$$

$$3x^2 - 12x^3 + 2$$

Reminders: tutoring TODAY

next assessment: Friday

Visually Random Grouping

- keeps things fresh
- collaborate with people you may not otherwise
- elimination of social barriers

$$-|x| \rightarrow -|x^0$$

Use the limit definition of derivative to find the slope of a line tangent to

$$f(x) = \underline{2x^2 - x + 1} \text{ at the point } (2, 7) \quad f' = \underline{4x - 1}$$

$$\lim_{\Delta x \rightarrow 0} \frac{f(x + \Delta x) - f(x)}{\Delta x}$$

$$\frac{2(x + \Delta x)^2 - (x + \Delta x) + 1 - (2x^2 - x + 1)}{\Delta x}$$

$$2(x^2 + 2x\Delta x + \Delta x^2) - x - \Delta x + 1 - 2x^2 + x - 1$$

$$\lim_{\Delta x \rightarrow 0} \frac{\cancel{2x^2} + 4x\Delta x + 2\Delta x^2 - \cancel{x} - \Delta x + 1 - \cancel{2x^2} + \cancel{x} - 1}{\Delta x}$$

$$\lim_{\Delta x \rightarrow 0} \frac{4x\Delta x + 2\Delta x^2 - \Delta x}{\Delta x} \Rightarrow \lim_{\Delta x \rightarrow 0} \frac{\cancel{\Delta x}(4x + 2\Delta x - 1)}{\cancel{\Delta x}}$$

$$\lim_{\Delta x \rightarrow 0} 4x + 2\Delta x - 1$$

$$4x + 2(0) - 1$$

$$f'(x) = \underline{4x - 1}$$

$$f'(2) = 4(2) - 1 = \textcircled{7}$$

The Derivative As a Function

$f(x)$: input number, output height (y-value) $f(2) = 7$

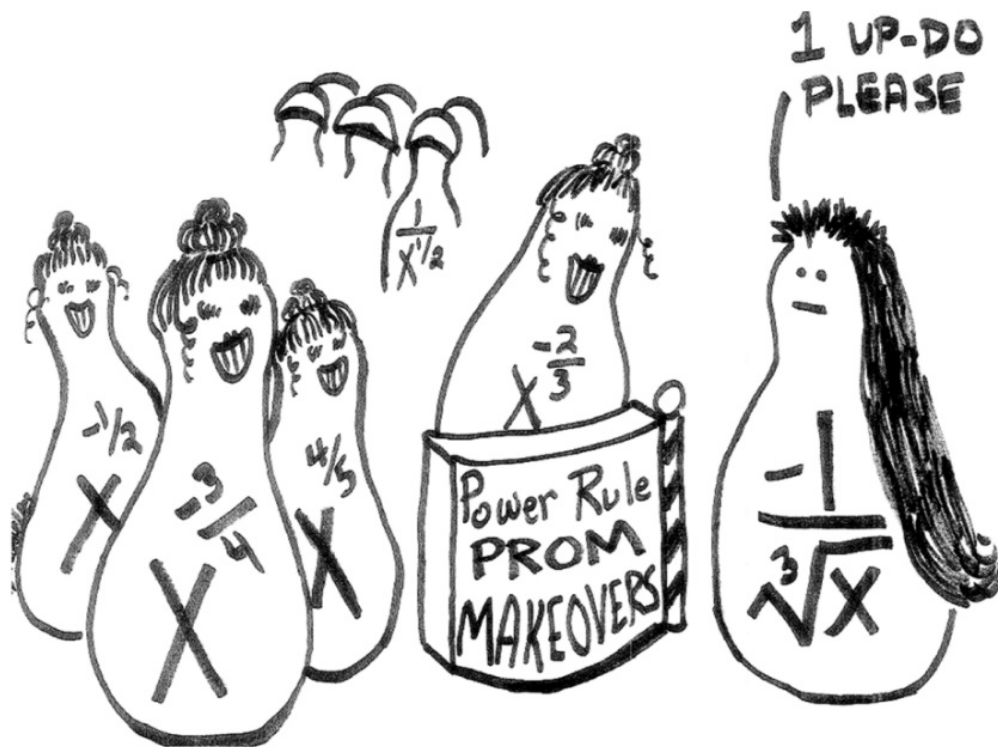
$$f(x) = 2x^2 - x + 1$$

$$\begin{array}{|c} 7 \\ \hline \end{array}$$

$f'(x)$: input number, output *Slope*.

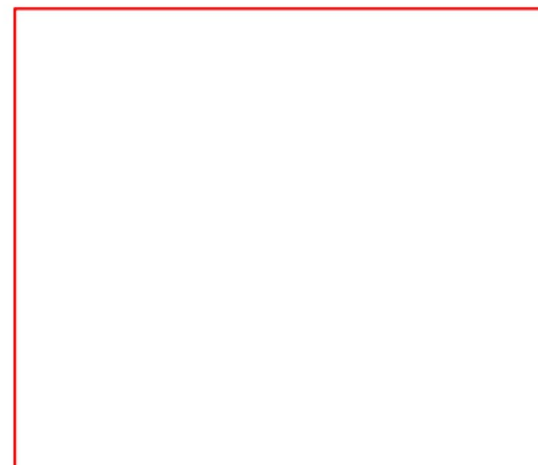
$$f'(x) = 4x - 1$$

$$\begin{aligned} f'(2) &= 4(2) - 1 \\ &= 7 \end{aligned}$$



To use the Power Rule
a function/term
must be in this form:

$$ax^n$$





$$-\frac{4}{\sqrt[3]{x^2}}$$



$$\frac{4}{x^{2/3}} \rightarrow -4x^{-2/3}$$

extreme makeover:
MATH EDITION



$$-4x^{-2/3}$$

CALCULUS \rightarrow

$$-4 \cdot \frac{-2}{3} x^{-5/3}$$
$$\downarrow$$
$$\frac{8}{3} x^{-5/3}$$
$$\frac{8}{3x^{5/3}}$$
$$\frac{8}{3\sqrt[3]{x^5}}$$

Find $f'(x)$ for $f(x) = \frac{3}{\sqrt[4]{x^5}}$

$$f(x) = 3 \cdot \frac{1}{x^{5/4}}$$

$$f(x) = 3 \cdot x^{-5/4}$$

power
rule

$$f'(x) = 3 \cdot \frac{-5}{4} x^{-9/4}$$

$$\frac{-15}{4} \cdot \frac{1}{x^{9/4}}$$

$$\Rightarrow \frac{15}{4 \sqrt[4]{x^9}}$$

$$\sqrt[a]{x^b} \Leftrightarrow x^{\frac{b}{a}}$$

$$x^{-n} \Leftrightarrow \frac{1}{x^n}$$

Due Weds:

p. 114 #5-18, 25-35

