

Good afternoon

Suppose a derivative is taken and the result is

$$f'(x) = \frac{6x}{3x^2-2} \quad \text{What was } f(x)?$$

$$\int \frac{1}{3x^2-2} 6x \, dx = \ln(3x^2-2) + C$$

$$f'(x) = \frac{1}{3x^2-2} \cdot 6x \quad f(x) = \ln(3x^2-2)$$

Write the equation of the line tangent to $y = \boxed{x^3} \boxed{e^{x^2}}$
at the point where $x=1$ (No calc)

$$y - y_1 = m(x - x_1)$$

$$y(1) = 1^3 e^{1^2} = e$$

$$y - e = m(x - 1)$$

$$y - e = 5e(x - 1)$$

$$\begin{aligned} f &: x^3 & g &: e^{x^2} \\ f' &: 3x^2 & g' &: e^{x^2} \cdot 2x \end{aligned}$$

$$\begin{aligned} y' &: 3x^2 e^{x^2} + 2x \cdot x^3 \cdot e^{x^2} \\ y'(1) &: 3 \cdot 1 \cdot e^1 + 2(1)(1)^3 \cdot e^{1^2} \\ &: 3e + 2e \end{aligned}$$

$$3e + 2e$$

$$5e$$

Reminders:

tutoring tomorrow 4-5p

assessment Friday

Rules from a table

| x | $f(x)$ | $f'(x)$ | $g(x)$ | $g'(x)$ |
|-----|--------|----------------|--------|---------|
| 1 | 2 | 2 | 1 | 1 |
| 2 | 4 | 0 | 2 | 1 |
| 3 | 2 | $-\frac{3}{2}$ | 3 | 1 |
| 4 | 1 | -1 | 4 | 1 |

Part 1) Given $h_1(x) = f(x) \cdot g(x)$, find $h_1'(4)$

Part 2) Given $h_2(x) = \frac{f(x)}{g(x)}$, find $h_2'(4)$

Part 3) Given $h_3(x) = (f(x))^2$, find $h_3'(2)$

Part 4) Given $h_4(x) = f(g(x))$, find $h_4'(2)$

$$\textcircled{1} h(x) = f(x)g(x)$$

$$h'(x) = f'(x)g(x) + f(x)g'(x)$$

$$h'(4) = f'(4)g(4) + f(4)g'(4)$$

$$(-1)(4) + (1)(1) \rightarrow -4 + 1 = \textcircled{-3}$$

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$$\textcircled{2} \quad h = \frac{f}{g}$$

$$h' = \frac{f'g - fg'}{g^2} : \frac{f'(4)g(4) - f(4)g'(4)}{g(4)^2}$$

$$\frac{-5}{(4)^2} = \textcircled{-5/16}$$

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$$\textcircled{3} h = (f(x))^2$$

$$h'(x) = 2(f(x)) \cdot f'(x)$$

$$h'(2) = 2(f(2)) f'(2)$$

$$2(4) \cdot 0 = 0$$

$\textcircled{4}$

$$h = f(g(x))$$

$$h' = f'(g(x)) \cdot g'(x)$$

$$h'(2) = f'(g(2)) \cdot g'(2)$$

$$f'(2) \cdot 1$$

$$0 \cdot 1$$

$$= \textcircled{0}$$