

Good afternoon: we will assess after answering some q's

If you don't feel ready today, you will need to assess  
Monday at 8:15a OR Monday DS or it becomes a zero to  
retake with hw!!!

If  $\frac{dy}{dx} = 2y^2$  and if  $y = -1$  when  $x = 1$ , then when  $x = 2$ ,  $y =$

$(1, -1)$

$(2, ?)$

$$\cancel{dx} \left( \frac{dy}{\cancel{dx}} = 2y^2 \right) dx$$

$$\frac{dy}{y^2} = \frac{2y^2 \cdot dx}{y^2}$$

$$\int y^{-2} dy = \int 2 dx$$

$$\frac{y^{-1}}{-1} + \cancel{C} = 2x + \cancel{C}$$

$$-\frac{1}{y} = 2x + C$$

$$\frac{1}{y} = -2x + C$$

$$y = \frac{1}{-2x + C} \rightarrow (1, -1) \rightarrow \left( -1 = \frac{1}{-2 + C} \right) -2 + C$$

$$y = \frac{1}{-2x + 1}$$

$$\underset{x=2}{y} = \frac{1}{-2(2) + 1} = \left( \frac{1}{-3} \right)$$

$$2 - C = 1$$

$$\underline{1 = C}$$

$$\frac{dy}{dx} = 3x^2$$

$$\int dy = \int 3x^2 \cdot dx$$

$$y = x^3 + C$$

$$\int \frac{1}{x} dx$$

$$x^{-1}$$

$$\frac{x^0}{0}$$

$$\int \frac{1}{x^4} dx$$

$$\int (x)^{-4}$$

$$x^{-3}$$

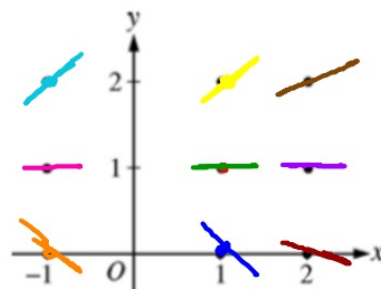
$$\frac{x^{-3}}{-3}$$

5. Consider the differential equation  $\frac{dy}{dx} = \frac{y-1}{x^2}$ , where  $x \neq 0$ .

(a) On the axes provided, sketch a slope field for the given differential equation at the nine points indicated.

(Note: Use the axes provided in the exam booklet.)

$(x, y)$	$\frac{dy}{dx}$
$(1, 1)$	0
$(2, 1)$	$\frac{0}{4} = 0$
$(-1, 2)$	$\frac{1}{1} = 1$
$(-1, 1)$	$\frac{0}{1} = 0$
$(-1, 0)$	$\frac{-1}{1} = -1$



(b) Find the particular solution  $y = f(x)$  to the differential equation with the initial condition  $f(2) = 0$ .

(c) For the particular solution  $y = f(x)$  described in part (b), find  $\lim_{x \rightarrow \infty} f(x)$ .

$(1, 2) \rightarrow \frac{1}{1} = 1$   
 $(2, 2) \rightarrow \frac{1}{4}$   
 $(1, 0) \rightarrow \frac{-1}{1} = -1$   
 $(2, 0) \rightarrow \frac{-1}{4}$