

4.6 The MVT and the FTC

FIND y' , THE DERIVATIVE OF THE FUNCTION y , FOR EACH OF THE FOLLOWING USING THE FUNDAMENTAL THEOREM OF CALCULUS.

924. $y = \int_0^x (t + 2) dt$

930. $y = \int_0^x t \cos t dt$

925. $y = \int_8^x \sqrt[3]{t} dt$

931. $y = \int_1^x \frac{t^2}{1+t^2} dt$

926. $y = \int_{\pi/4}^x \sec^2 t dt$

932. $y = \int_x^{x+2} (4t + 1) dt$

927. $y = \int_{-2}^x (t^2 - 2t) dt$

933. $y = \int_0^{\sin x} \sqrt{t} dt$

928. $y = \int_{-1}^x \sqrt{t^4 + 1} dt$

934. $y = \int_0^{x^3} \sin(t^2) dt$

929. $y = \int_0^x \tan^4 t dt$

935. $y = \int_0^{3x} \sqrt{1+t^3} dt$

FIND THE AVERAGE VALUE OF EACH OF THE FOLLOWING FUNCTIONS ON THE GIVEN INTERVAL.

936. $f(x) = x - 2\sqrt{x}$; $[0, 2]$

938. $f(x) = 2 \sec^2 x$; $[-\frac{\pi}{4}, \frac{\pi}{4}]$

937. $f(x) = \frac{9}{x^3}$; $[1, 3]$

939. $f(x) = \cos x$; $[-\frac{\pi}{3}, \frac{\pi}{3}]$

FIND EXACT VALUES FOR EACH OF THE FOLLOWING DEFINITE INTEGRALS.

940. $\int_0^1 (x^2 + \sqrt{x}) dx$

947. $\int_0^3 (3x^2 + x - 2) dx$

941. $\int_0^{\pi/3} 2 \sec^2 x dx$

948. $\int_1^2 \left(\frac{3}{x^2} - 1 \right) dx$

942. $\int_{-\pi/2}^{\pi/2} (8y^2 + \sin y) dy$

949. $\int_{-2}^{-1} \left(u - \frac{1}{u^2} \right) du$

943. $\int_4^9 \frac{1 - \sqrt{u}}{\sqrt{u}} du$

950. $\int_{-\pi/3}^{\pi/3} 4 \sec \theta \tan \theta d\theta$

944. $\int_2^7 3 dx$

951. $\int_0^2 3^x \ln 3 dx$

945. $\int_{-1}^8 (x^{1/3} - x) dx$

952. $\int_0^{\ln 5} e^x dx$

946. $\int_{-1}^1 (t^2 - 2) dt$

953. $\int_{-1}^1 \frac{1}{\sqrt{1-x^2}} dx$