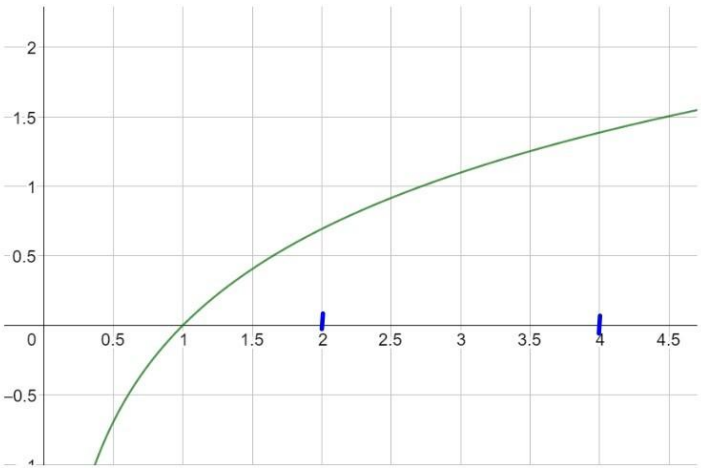
Good afternoon: for the warm up, finish the task from DS

Approximate $\int_2^4 \ln x \, dx$ using 4 midpoint rectangles



$\Delta x = \frac{4-2}{4} = 0.5$

Subintervals ← midpts

2 to 2.5: 2.25

2.5 to 3: 2.75

3 to 3.5: 3.25

3.5 to 4: 3.75

(fire drill? second level, speed bump)

$0.5\left(f(2.25)+f(2.75)+f(3.25)+f(3.75)\right)$

$=$ [ ]

CIM

$$\int_2^4 \ln x \, dx$$

these numbers are x-values

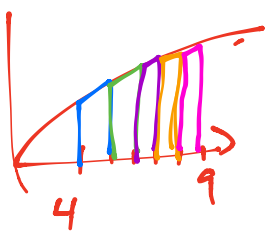
Approximate $\int_4^9 \sqrt{x}\,dx$ using 5 trapezoids of equal width.

$\Delta x = \frac{9-4}{5} = 1$

$\frac{\Delta x}{2}\left[f(x_0) + 2\left[f(x_1) + \cdots\right] + f(x_n)\right]$

$\frac{1}{2}\left[\sqrt{4} + 2\left[\sqrt{5} + \sqrt{6} + \sqrt{7} + \sqrt{8}\right] + \sqrt{9}\right]$

≈ 12.660



$$\frac{\Delta x}{2}\left[f(x_0) + 2\left[f(x_1) + \ldots + f(x_{n-1})\right] + f(x_n)\right]$$

Suppose f is a continuous function with the selected values below. Approximate the integral using 4 rectangles, LRAM and RRAM.

$$\int_0^8 f(x)\,dx$$

1 2 3 2 ← varying Δx's

x	0	1	3	6	8
$f(x)$	5	4	5	4	5

LRAM

$\approx 5\cdot 1 + 4\cdot 2 + 5\cdot 3 + 4\cdot 2$

$5 + 8 + 15 + 8$

36

RRAM: $f(x)\,\Delta x$

$4\cdot 1 + 5\cdot 2 + 4\cdot 3 + 5\cdot 2$

$4 + 10 + 12 + 10$

$= 36$

Why do it from a table?
We don't always have all the values, or a specific function that models behavior--just data.

Especially useful for position-velocity-acceleration

Riemann Definition of Definite Integral

"definite Integral"

$$\Delta x = \frac{b-a}{n} \qquad \lim_{n\to\infty} \sum_{i=1}^{n} f(x_i)\Delta x = \int_a^b f(x)\,dx$$

- Δx: width of 1 rect.
- $b-a$: interval width
- n: # of rectangles
- $\lim_{n\to\infty}$: ∞ many rect.; very thin width
- $\sum_{i=1}^{n}$: Area of n rectangles
- $f(x_i)\Delta x$: area of i^{th} rectangle
- $f(x_i)$: height of i^{th} rectangle
- Δx: width
- $\int_a^b f(x)\,dx$: exact area under $f(x)$ between a & b

Be fluent algebraically:

Write a definite integral whose value equals

$$\lim_{n\to\infty} \sum_{i=1}^{n} \left[\left(3+\frac{5}{n}i\right)^3+\left(3+\frac{5}{n}i\right)^2-4\right]\frac{5}{n}$$

Δx

so, $b-a=5$

$b=a+5$

varies as i increases to n; starts @ 3. this is x

3 is a starting value

$$\int_3^8 x^3+x^2-4\,dx$$

Write a definite integral whose value equals

$$\lim_{n\to\infty} \sum_{i=1}^{n} \sin\left(6+\frac{2i}{n}\right)\frac{2}{n}$$

$\frac{2i}{n}$: x

$\frac{2}{n}$: $b-a$

6 : a

Δx

if $b-a=2$
then $b=a+2$
$\rightarrow a=6$
so $b=8$

$$\int_6^8 \sin(x)\,dx$$

Write an infinite Riemann sum whose value equals

$$\int_5^8 \sqrt{x+3}\,dx$$

$b-a = 3$

a

$$\lim_{n\to\infty} \sum_{i=1}^{n} \sqrt{\left(5+\frac{3}{n}i\right)+3}\,\frac{3}{n}$$

x

$a + \Delta x i$

https://www.desmos.com/calculator/wlo7qlygfi

Write an infinite Riemann sum whose value equals

$$\int_2^7 e^{3x}\,dx$$

$$\lim_{n\to\infty} \sum_{i=0}^{n} e^{3\left(2+\frac{5i}{n}\right)} \frac{5}{n}$$