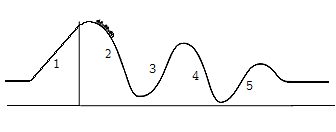
**Roller Coaster Project**

Due: 4/30

Groups: 1-3 people

Goal: Design a roller coaster using at least 5 piecewise functions that is everywhere continuous and differentiable. Turn in: functions, calculations, 3D paper model, and poster-sized hand-drawn graph of roller coaster with each piece of the function clearly labeled. (May use graph paper taped together, 3 sheets by 2 sheets size.)



Example. Suppose our roller coaster starts up the “lift ramp” defined by when The graph of this equation looks like this:



\*\*TI-TIP: Inequality signs can be found in 2nd Math (Test). You can also set your domain such as by typing in . “and” statements are also found in 2nd Math (Test) 🡪 Logic.

We need to develop a curve which is both continuous and differentiable at x = 0. Let’s suppose it is a downward parabola in the form of

We know that in order to be continuous, then so and

In order for to be differentiable, then must equal the slope of at   
So and when

So You can assign to be any value you wish. Since it is to open downward, let

So Here is the graph and a zoom to show continuity and differentiability.



Here is another example.   
Suppose you have Y2 as and you wish to connect it with another parabola (hopefully). So is the point where your new parabola is going to begin.

Let us define our new parabola Y3 in the form It will become apparent in a minute why I want to do that. Our goal is to find and

Now we want Y2 and Y3 to be continuous at   
 by plugging in. . So One piece of the puzzle solved!

Now we want Y2 and Y3 to be differentiable at   
 so so

Since they must be the same, then The second piece of the puzzle!

Now can be anything you want. Since it will open up, must be positive. For now, try

So your Graph this for

Note that this goes way below the axis. So play around with the value of , making it smaller, like 0.5 (You may have to play around with the window as well). You can adjust it to anything you want. Remember though that the -axis really means nothing. Don’t think that the coaster has to start on the -axis. To start it lower, just make your XMIN a smaller number. You might actually want to turn the axes off in your 2nd Format screen.

Hopefully you see why I chose the parabola in the format. It makes it far easier to work with because of the fact that when many of the terms wash out. So if your 4th curve was a parabola which needed to start at your If it was a cube, it would be in the form If it were an exponential, it would be .

Finally, once you have your Y3, you may want to *foil* it out and collect terms so it looks “nicer”.

\* \* \*

In this project, you need at least 5 piecewise functions showing a possible roller coaster. You need to show the graph and a proof that the function you generate is continuous and differentiable at the points where the curves split into each piece. You may use any type of function we have discussed including linear, trig, exponential, logarithms, inverse trig, and polynomial.

Products to turn in:

1. Paper with functions in piecewise form with full equations and calculations showing continuity and differentiability at transition points.
2. (electronically produced) Graph of functions with which to create 3D model (explained in class)
3. Poster sized graph of functions: posters should have each function equation included with the appropriate part of the roller coaster. Transition points should be clearly marked and given as an ordered pair. Be sure to name your coaster something exciting!

**Remember:** (1) Roller coasters should start and end at same height. You many want to use a horizontal line as your loading area. This does not count as one of the curves. (2) Roller coasters do not go as high as their previous maximum. (3) Can you put in a loop?! Not necessary, but would be very cool…