

Evaluate each limit. Show all work. If a limit does not exist, show why.

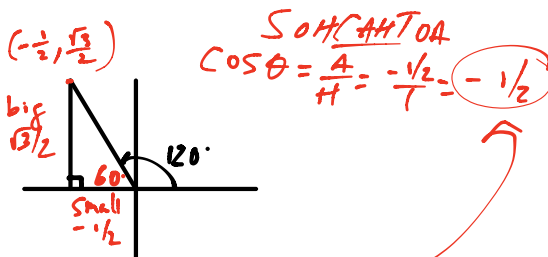
1.  $\lim_{x \rightarrow -1} \frac{x^2 + 5x + 4}{x + 1} = \frac{1 - 5 + 4}{-1 + 1} = \frac{0}{0}$  😞

💡  $\lim_{x \rightarrow -1} \frac{(x+4)(x+1)}{x+1} \rightarrow \lim_{x \rightarrow -1} \frac{(x+4)\cancel{(x+1)}}{\cancel{x+1}} \rightarrow \lim_{x \rightarrow -1} x+4 = -1+4 = \boxed{3}$

2.  $\lim_{x \rightarrow 2} \frac{x-2}{x^2-x-2} = \frac{2-2}{4-2-2} = \frac{0}{0}$  😞

$\lim_{x \rightarrow 2} \frac{x-2}{(x+1)\cancel{(x-2)}} = \lim_{x \rightarrow 2} \frac{1}{x+1} = \frac{1}{2+1} = \boxed{\frac{1}{3}}$

3.  $\lim_{x \rightarrow -1} \frac{x^2 - 2x}{x} = \frac{1 - 2(-1)}{-1} = \frac{1+2}{-1} = \frac{3}{-1} = \boxed{-3}$  (11) / \



4.  $\lim_{x \rightarrow \frac{\pi}{3}} \cos(2x) = \cos\left(\frac{2\pi}{3}\right)$

↳  $\pi/3 = 60 \dots$  so  $2\pi/3 = 120$ ! 🙄

5.  $\lim_{x \rightarrow 3} \frac{\sqrt{x+1}-2}{3-x} = \frac{2-2}{3-3} = \frac{0}{0}$  😞

$\lim_{x \rightarrow 3} \frac{(\sqrt{x+1}-2) \cdot (\sqrt{x+1}+2)}{(3-x) \cdot (\sqrt{x+1}+2)}$   
 "Foil" Distribute

$\lim_{x \rightarrow 3} \frac{x+1-4}{(3-x)(\sqrt{x+1}+2)}$

$\lim_{x \rightarrow 3} \frac{x-3}{(3-x)(\sqrt{x+1}+2)}$  😞

$\lim_{x \rightarrow 3} \frac{-1(3-x)}{\cancel{(3-x)}(\sqrt{x+1}+2)}$

$\lim_{x \rightarrow 3} \frac{-1}{\sqrt{3+1}+2} = \frac{-1}{\sqrt{4}+2} = \frac{-1}{2+2} = \boxed{-\frac{1}{4}}$

SELF: F-L2a

Use the graph of  $f(x)$  shown here for #5-9.

Tell whether each is true or false. If false, explain why.

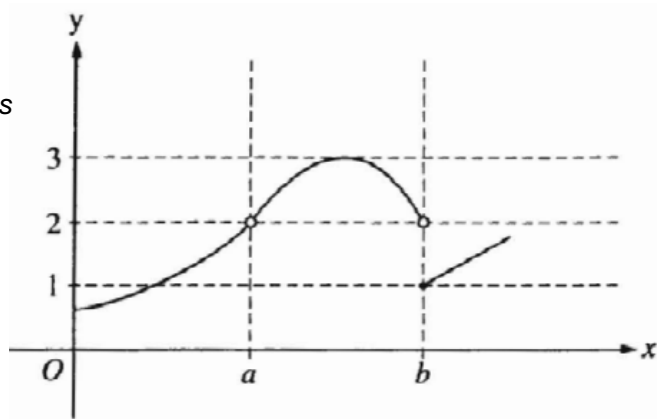
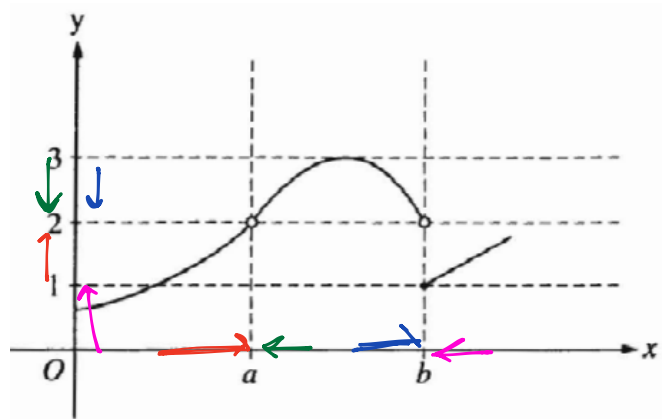
6.  $\lim_{x \rightarrow a} f(x) = \lim_{x \rightarrow b} f(x)$  *False. The limit at  $a$  is 2 and the limit at  $b$  does not exist because  $2 \neq 1$*

7.  $\lim_{x \rightarrow a} f(x) = 2$  *True*

8.  $\lim_{x \rightarrow b} f(x) = 2$  *False. From the left of  $b$ ,  $f$  approaches 2 and from the right of  $b$   $f$  approaches 1.*

9.  $\lim_{x \rightarrow b} f(x) = 1$  *False. While  $f(b)=1$ , the limit does not exist.*

10.  $\lim_{x \rightarrow a} f(x)$  does not exist



*False. From the right of  $a$ ,  $f$  approaches 2. From the left of  $a$ ,  $f$  approaches 2. Since  $2=2$ , the limit exists.*