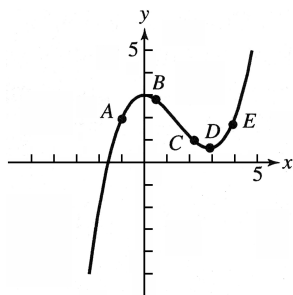


Advanced Placement Calculus AB Test

Section I—Part A (55 minutes)

Choose the best answer for each question. Your score is determined by subtracting one-fourth of the number of wrong answers from the number of correct answers. **Calculators are not permitted.**

1.



For the graph shown, at which point is it true that $\frac{dy}{dx} < 0$ and $\frac{d^2y}{dx^2} < 0$?

- (A) A (B) B (C) C (D) D (E) E

2. Find the area of the region bounded by the x -axis and the graph of $y = (x+1)(x-2)^2$.

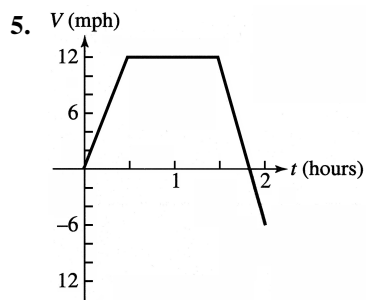
- (A) $\frac{5}{4}$ (B) $2\frac{3}{4}$ (C) $5\frac{1}{4}$ (D) $6\frac{1}{4}$ (E) $6\frac{3}{4}$

3. Which of the following is an antiderivative of $x^2 \sec^2 x^3$?

- (A) $2x \sec^2 x^3 + 6x^4 \sec^2 x^3 \tan x^3$
 (B) $2x \sec^2 x^3 + 6x^3 \sec x^3$
 (C) $\frac{1}{3} \tan x^3 - 5$
 (D) $3 \tan x^3 + \pi$
 (E) $-\frac{1}{3} \cot x^3 + 4$

4. Line L is tangent to the curve defined by $2xy^2 - 3y = 18$ at the point $(3, 2)$. The slope of line L is

(A) $\frac{21}{8}$ (B) $\frac{32}{3}$ (C) $-\frac{10}{21}$ (D) $\frac{8}{21}$ (E) $-\frac{8}{21}$



A bicyclist rides along a straight road starting from home at $t = 0$. The graph above shows the bicyclist's velocity as a function of t . How far from home is the bicyclist after 2 hours?

(A) 13 miles (B) 16.5 miles (C) 17.5 miles (D) 18 miles (E) 20 miles

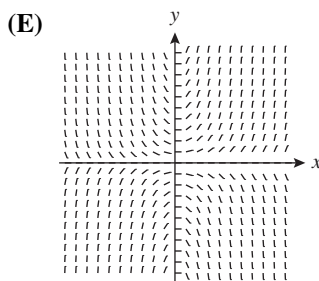
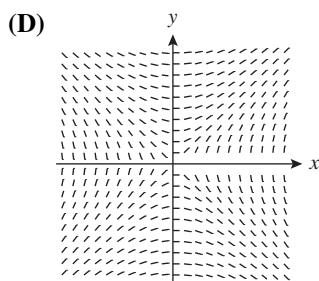
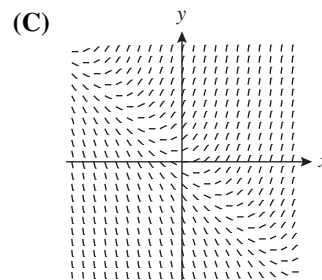
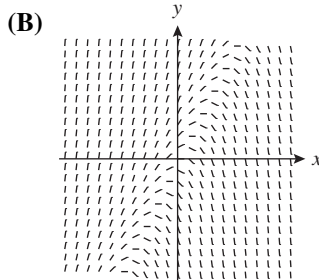
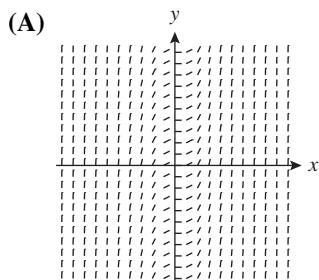
6. Find the value of x at which the graph of $y = \frac{1}{x} + \sqrt{x}$ has a point of inflection.

(A) 2 (B) $4^{2/3}$ (C) 4 (D) 6 (E) 8

7. Find $\lim_{x \rightarrow \infty} \frac{2x - 4x^3}{8x^3 + 4x^2 - 3x}$.

(A) $\frac{2}{3}$ (B) $\frac{3}{2}$ (C) 1 (D) $-\frac{1}{2}$ (E) $-\frac{3}{4}$

8. Which of the following is a slope field for the differential equation $\frac{dy}{dx} = -2x + y$?



9. Let $f(x) = \cos(3\pi x^2)$. Find $f'\left(\frac{1}{3}\right)$.

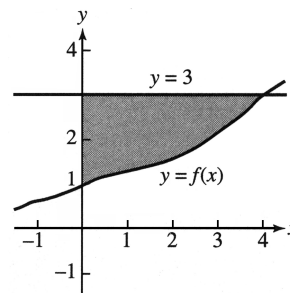
(A) $-\sqrt{3}\pi$ (B) $\sqrt{3}\pi$ (C) 0 (D) $-\frac{\sqrt{3}\pi}{2}$ (E) $-\pi$

10. Assume that $f(x)$ is a one-to-one function. The area of the shaded region is equal to which of the following definite integrals?

I. $\int_0^4 [f(x) - 3] dx$

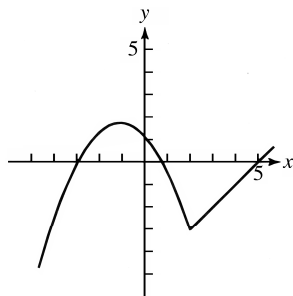
II. $\int_4^0 [f(x) - 3] dx$

III. $\int_1^3 f^{-1}(y) dy$



(A) I only (B) II only (C) III only (D) I and III (E) II and III

11.



The graph of a function $y = f(x)$ is shown above. Which of the following are true for the function f ?

I. $f'(2)$ is defined.

II. $\lim_{x \rightarrow 2^+} f(x) = \lim_{x \rightarrow 2^-} f(x)$

III. $f'(x) < 0$ for all x in the open interval $(-1, 2)$.

(A) I only

(B) II only

(C) III only

(D) II and III

(E) I, II and III

12. Let $f(x) = \sin^{-1} x$. Find $f'\left(\frac{\sqrt{2}}{2}\right)$.

(A) $\frac{\pi}{4}$

(B) $\frac{\sqrt{2}}{2}$

(C) $\frac{1}{2}$

(D) $\sqrt{2}$

(E) Undefined

13. Evaluate $\int (\cos x - e^{2x}) dx$.

(A) $-\sin x - \frac{1}{2}e^{2x} + C$

(B) $\sin x - \frac{1}{2}e^{2x} + C$

(C) $-\sin x - 2e^{2x} + C$

(D) $\sin x - 2e^{2x} + C$

(E) $-\cos x - \frac{1}{2}e^{2x} + C$

14. Let $f(x) = e^{x^3 - 2x^2 - 4x + 5}$. Then f has a local minimum at $x =$

(A) -2 (B) $-\frac{2}{3}$ (C) $\frac{2}{3}$ (D) 1 (E) 2

15. The acceleration of a particle moving along the x -axis is $a(t) = 12t - 10$.

At $t = 0$, the velocity is 4.

At $t = 1$, the position is $x = 8$.

Find the position at $t = 2$.

(A) 5 (B) 4 (C) 10 (D) 11 (E) 7

16. Let f be differentiable for all real numbers. Which of the following must be true for any real numbers a and b ?

I. $\int_2^a f(x) dx = \int_2^b f(x) dx + \int_b^a f(x) dx$

II. $\int_a^b ([f(x)]^2 + f'(x)) dx = [f(b)]^2 - [f(a)]^2$

III. $\int_a^b 3f(x) dx = 3 \int_a^b f(x) dx$

(A) I only (B) II only (C) I and II (D) I and III (E) I, II, and III

17. Find an equation of the line normal to the graph of $y = \frac{3x}{x^2 - 6}$ at $x = 3$.

(A) $5x + y = 18$ (B) $5x - y = 12$ (C) $5x + 3y = 24$ (D) $x - 5y = -12$ (E) $x + y = 6$

18. Let $g(x) = \lim_{h \rightarrow 0} \frac{(x+h)^2 - x^2}{h}$. For what value of x does $g(x) = 2$?

- (A) $x = 1$ (B) $x = 2$ (C) $x = 3$ (D) $x = 4$ (E) $x = 5$
-

19. Let f be a differentiable function of x that satisfies $f(1) = 7$ and $f(4) = 3$. Which of the following conditions would guarantee that the tangent line at $x = c$ is parallel to the secant line joining $(1, f(1))$ to $(4, f(4))$?

- (A) $f(c) = \frac{3}{2}$ (B) $f(c) = 5$ (C) $f'(c) = -\frac{3}{4}$ (D) $f'(c) = -\frac{4}{3}$ (E) $f(c) = -\frac{4}{3}$
-

20. Let $f(x) = x^3 - 12x$. Which statement about this function is false?

- (A) The function has a relative minimum at $x = 2$.
(B) The function is increasing for values of x between -2 and 2 .
(C) The function has two relative extrema.
(D) The function is concave upward for $x > 0$.
(E) The function has one inflection point.
-

21. $\int_2^3 8x(x^2 - 5)dx =$

- (A) $\frac{74}{3}$ (B) 30 (C) 90 (D) 112 (E) $\frac{370}{3}$
-

22. Let $f(x) = \frac{d}{dx} \int_0^x \sqrt{t^2 + 16} dt$. What is $f(-3)$?

- (A) -5 (B) -4 (C) 3 (D) 4 (E) 5
-

23. If $\frac{dy}{dx} = xy^2$ and $y = -\frac{1}{3}$ when $x = 2$, what is y when $x = 4$?

- (A) $-\frac{1}{3}$ (B) $-\frac{1}{5}$ (C) $-\frac{1}{9}$ (D) $\frac{1}{3}$ (E) $\frac{1}{9}$

62 Sample AB Test

24. Use the Trapezoidal Rule with $n = 3$ to approximate the area between the curve $y = x^2$ and the x -axis for $1 \leq x \leq 4$.

(A) 14 (B) 21 (C) 21.5 (D) 29 (E) 30

25. Let $f(x)$ be a continuous function that is defined for all real numbers x .

If $f(x) = \frac{x^2 - x - 6}{x^2 - 5x + 6}$ when $x^2 - 5x + 6 \neq 0$, what is $f(3)$?

(A) 5 (B) 4 (C) 2 (D) 1 (E) 0

26. Find the derivative of $\cos^3 2x$.

(A) $-\sin^3 2x$
(B) $-6\cos^2 2x$
(C) $6\cos^2 2x \sin 2x$
(D) $-3\cos^2 2x \sin 2x$
(E) $-6\cos^2 2x \sin 2x$

27. Let f be a twice-differentiable function whose derivative $f'(x)$ is increasing for all x . Which of the following must be true of all x ?

I. $f(x) > 0$
II. $f'(x) > 0$
III. $f''(x) > 0$

(A) I only (B) II only (C) III only (D) I and II (E) II and III

28. The function $f(x) = x^3 - 6x^2 + 9x - 4$ has a local maximum at

(A) $x = 0$ (B) $x = 1$ (C) $x = 2$ (D) $x = 3$ (E) $x = 4$